

**Fuzzy approximate entropy analysis of resting state fMRI signal  
complexity across the adult life span**

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## Abstract

In this study, we present a method for measuring functional magnetic resonance imaging (fMRI) signal complexity using fuzzy approximate entropy (fApEn) and compare it with the established sample entropy (SampEn). Here we use resting state fMRI dataset of 86 healthy adults (41 males) with age ranging from 19 to 85 years. We expect the complexity of the resting state fMRI signals measured to be consistent with the Goldberger/Lipsitz model for robustness where healthier (younger) and more robust systems exhibit more complexity in their physiological output and system complexity decrease with age. The mean whole brain fApEn demonstrated significant negative correlation ( $r = -0.472$ ,  $p < 0.001$ ) with age. In comparison, SampEn produced a non-significant negative correlation ( $r = -0.099$ ,  $p = 0.367$ ). fApEn also demonstrated a significant ( $p < 0.05$ ) negative correlation with age regionally (frontal, parietal, limbic, temporal and cerebellum parietal lobes). There was no significant correlation regionally between the SampEn maps and age. These results support the Goldberger/Lipsitz model for robustness and have shown that fApEn is potentially a sensitive new method for the complexity analysis of fMRI data.

**Keywords:** Ageing, Blood oxygen level dependent (BOLD), Complexity, Fuzzy approximate entropy (fApEn), resting state-functional magnetic resonance imaging (rs-fMRI), Sample entropy (SampEn).

### Highlights

- The method for fMRI signal complexity analysis using fApEn is presented.
- fApEn significantly associated with age.
- The fApEn-ageing effect in white matter and gray matter are both significant.
- These results support the Goldberger/Lipsitz model for complexity and robustness.
- fApEn is a potentially reliable method for the complexity analysis of fMRI data.

## 1. Introduction

Discovering how we age and identifying the proxies of successful ageing is becoming important as the population ages in the developed world. Biological systems theory suggests that physiological ageing is associated with a generalized loss of complexity in the dynamics of healthy system and hypothesize that such loss of complexity leads to an impaired ability to adapt to physiologic stress, resulting in a functional loss and deficit [1]. We have previously demonstrated that this is true in the brain using the blood oxygen level dependent (BOLD) fMRI signal [2]. However, the measurement of complexity in fMRI is difficult due to the limited temporal resolution and the length of the signal acquisitions possible (data length).

The subtle patterns and changes in the signals produced by the short and noisy sequences of real physiological data, from sophisticated biomedical systems are often undetected by nonlinear signal processing measures like correlation dimension [3] and Lyapunov exponent [4]. These nonlinear measures usually require a large data set [5] and assume that the signals produced by biomedical systems are time-invariant (output signal does not depend explicitly on time) [6]. Biomedical systems like the human brain have nonlinear and chaotic properties and the signals they produce are dynamic in nature [7]. Conceptually, the integral of the sum of all the positive characteristic Lyapunov exponents gives an estimate of the Kolmogorov-Sinai entropy (KS entropy) [8]. Also, the Lyapunov spectrum can be used to give an estimate of the rate of entropy production, fractal dimension and information dimension [9]. KS entropy was developed to classify deterministic dynamic systems by rates of information generation [10] where absence of noise and infinite data length are standard mathematical assumptions. As a result, it is compromised by noise and short data length [11]. Other signal processing measures such as spectral and autocorrelation analyses achieve minimal distinctions in both stochastic processes and noisy deterministic data sets [12]. The

quantification and analysis of these undetected signal changes reflect underlying biological mechanisms and may provide fundamental insights into the nature of these processes and their understanding may lead to clinical and biomedical applications targeted at maintaining resilience or robustness.

To solve the problem of undetected signal changes in short and noisy datasets obtained from biomedical systems, Pincus proposed a family of statistics called approximate entropy (ApEn) [13], for measuring signal complexity. Here, complexity can be described as the presence of similar patterns in a signal. ApEn is defined as an approximation to the Kolmogorov complexity [14] and is in the same conceptual frame as KS entropy but with a different view of providing a widely applicable statistical formula to distinguish data sets that are composites of both deterministic and stochastic processes [11]. Given  $N$  data length and tolerance  $r$ ,  $\text{ApEn}(m, r, N)$  is approximately equal to the negative average natural logarithm of the conditional probability that two sequences, which are similar for  $m$  points within the tolerance remain similar at the next point [13, 15]. ApEn has been applied to a wide range of biomedical signals such as hormone pulsatility [16], genetic sequences [17], respiratory patterns [18], heart rate variability [19], electrocardiograms [20], electroencephalograms (EEG) [21], magnetoencephalograms (MEG) [22] and functional magnetic resonance imaging data (fMRI) [2]. Correlation dimension and KS entropy employ embedding dimension  $m$ , like ApEn, but ApEn can be applied to biomedical settings where correlation dimension and KS entropy are either undefined or infinite with good replicability properties [11]. However, the ApEn algorithm counts each sequence as matching itself to avoid the occurrence of  $\ln(0)$  in the calculations, which led to the bias of ApEn [11]. This bias causes ApEn to be heavily dependent on data length, makes it uniformly lower than expected for short data lengths and lack relative consistency.

Sample entropy (SampEn) was introduced as an improvement of ApEn where self-matches are excluded, i.e. vectors are not compared to themselves so as to reduce the bias of ApEn [23]. SampEn is the negative natural logarithm of the conditional probability that two sequences remain similar at the next point, where self-matches are not included in calculating the probability [23]. Hence, a lower value of SampEn also indicates more self-similarity and less complexity in the time series. SampEn is largely independent of data length and displays relative consistency over a broader range of possible parameters ( $m$ ,  $r$  and  $N$ ) under circumstances where ApEn does not [23]. Likewise, SampEn has been applied on a single scale and multi scale level in a number of biomedical signals such as EEG [24], MEG [25] and functional magnetic resonance imaging data (fMRI) [26, 14, 27, 28, 29]. In fact, due to its superior discriminatory ability it has become an established measure of signal complexity in most biomedical signals, especially fMRI signals which typically comprise short and noisy data sets. Irrespective of the superior properties SampEn exhibit in comparison to ApEn, it also has a limitation. SampEn ( $m$ ,  $r$ ,  $N$ ) is not defined for signals if no template and forward match occurs (which may occur in signals with small  $r$  and  $N$  values) [23].

Recently, another improved version of approximate entropy that also measures signal complexity, called Fuzzy approximate entropy (fApEn) has been proposed [30, 15]. In fApEn, Zadeh's concept of "fuzzy sets" was incorporated into the standard ApEn, to obtain a fuzzy measurement of the similarity between the difference  $d|X_i, X_j|$ , of any pair, of corresponding  $m$  measurements of  $X_i$  and  $X_j$  based on their shapes. In comparison to standard ApEn and SampEn using independent, identically distributed (i.i.d) Gaussian and uniform noise, fApEn with respect to standard ApEn showed better monotonicity, relative consistency, and robustness to noise when characterising signals with different complexities

[15]. In comparison to SampEn, fApEn was not limited by the tolerance,  $r$  as in the calculation of SampEn [30, 15]. Xie et al [15] further characterised fApEn and ApEn with experimental electromyography (EMG) signals and found that fApEn significantly decreased during the development of muscle fatigue, which is a similar trend to that of the mean frequency of the EMG signal, while the standard ApEn failed to detect this change. Also, fApEn has been applied to other studies of EMG [31] and EEG [32]. To the best of our knowledge, the application of fApEn to analyse experimental BOLD fMRI signals remain unexplored.

Here, we investigate the performance and characteristics of fApEn on fMRI signal complexity and evaluate its potential for complexity analysis of fMRI data. To assess the appropriateness and effectiveness of fApEn for fMRI signal complexity analysis we compared it to the well-established SampEn analysis using resting state fMRI data of healthy adults with age ranging from 19 to 85 years. Here, we investigated the association between fApEn and age, and SampEn and age. BOLD fMRI signal is a good candidate for fApEn and SampEn analysis because it has poor temporal resolution (relatively few time points) and is inherently noisy.

The BOLD signal is an indirect measure of neural activity in the human brain. The haemodynamic response efficiency (HRE) is an index of the coupling between neural activity and vascular response [33]. Hemodynamic response in gray matter is higher than in white matter [33]. As a result of this, BOLD fMRI studies have mainly focused on gray matter. However, BOLD fMRI activations in white matter have been reported in many other studies and this continue to increase [34].



The characterization and analysis of a system's output complexity may give an indication of its health and robustness. [35, 36, 37]. Systems with complex output patterns are thought to be better able to adapt to perturbation and damage, minimising functional loss. Adaptability is the capacity to respond to unpredictable perturbation and stresses, and this is a defining feature of healthy function. A loss of adaptive capacity in complex physiological systems can be characterized as a manifestation of the degradation of multiple physiological processes that are normally responsible for healthy adaptation to daily stresses. The degradation of these processes with age and disease can be observed as a loss of complexity in the dynamics of complex physiological systems [1].

As we age there is a decline in cognitive abilities such as processing speed, memory, executive function and reasoning [38]. The basis for this decline is not well understood, although it is reasonable to assume that its pathological origin is the accumulation of a variety of age and disease specific pathologies. How the brain overcomes the effects of this pathological burden to maintain function is unclear. The complexity of fMRI signals using entropy has been shown to vary with age and may represent a decrease [26] or increase in the capacity to adapt to the accumulation of age-related pathologies [2, 39]. In the present analyses, we expect the complexity of the resting state fMRI signal measured by fApEn and SampEn to be consistent with the Goldberger/Lipsitz model for robustness [35, 36, 37, 1] where healthier and more robust systems exhibit more complexity in their physiological output and system complexity decrease with age. Also, we expect fApEn to exhibit at least similar performance and discriminatory ability to SampEn, a well-established method in fMRI signal complexity analysis [26, 14, 27, 28, 29].

## 2. Materials and Methods

### 2.1 Participants

The International Consortium for Brain Mapping (ICBM) resting state dataset made publicly available in the 1000 Functional Connectomes project was used for this investigation. The ages of the 86 healthy adults' (41 males) ranged from 19 to 85 years (mean age of  $44.19 \pm 17.92$  years). The study was approved by the local research ethics committee and subjects had no history of neurological or psychiatric disorders. Written informed consent was obtained from the subjects. Information regarding this dataset is available at [https://www.nitrc.org/projects/fcon\\_1000/](https://www.nitrc.org/projects/fcon_1000/).

### 2.2 Brain imaging

Subjects were asked to lie in the scanner with their eyes closed during fMRI acquisition on a 3T scanner, using a  $T_2^*$  weighted gradient echo echo-planar imaging sequence (EPI) and a standard head coil. A total of 23 axial slices were obtained for each of 133 volumes using a TR of 2 s and matrix 64x64. A total of 128 volumes of fMRI data remained after discarding the first five volumes to allow for signal conditioning.

### 2.3 Image pre-processing

SPM8 software (The Wellcome Department of Imaging Neuroscience, UCL, London, UK) was used for the fMRI data pre-processing. The images were realigned to correct for head movement. Using the first level analysis of SPM8, temporal high pass filtering was

performed at 128 seconds to reduce low frequency noise and the six head movement parameters obtained after realignment were regressed as covariates of no interest. Each voxel time series was standardised to a mean of zero and standard deviation of unity. This allowed a signal value of  $r$  (tolerance) to be used for all voxels independent of amplitude and variance. Spatial smoothing was performed on the entropy maps before regional analysis to reduce white noise using a Gaussian smoothing kernel with full-width at half maximum (FWHM) [8 8 8].

## 2.4 Standard ApEn algorithm

ApEn is defined for a given N-dimensional signal  $(x_1, x_2, \dots, x_N)$  as:

$$ApEn(m, r, N) = \Phi^m(r) - \Phi^{m+1}(r)$$

where

$$\Phi^m(r) = [N - (m-1)\tau]^{-1} \sum_{i=1}^{N-(m-1)\tau} \ln[C_i^m(r)] \quad (1)$$

and

$$C_i^m(r) = \frac{1}{N - (m-1)\tau} \sum_{j=1}^{N-(m-1)\tau} \Theta(d_{ij}^m - r) \quad (2)$$

In Eq. (1),  $N$  is the number of time points;  $m$  specifies the pattern length and  $\tau$  is the time delay. In Eq. (2), the symbol  $\Theta$  is the Heaviside function, given as

$$\Theta(z) = \begin{cases} 1 & \text{if } z \leq 0 \\ 0 & \text{if } z > 0 \end{cases}$$

The distance  $d_{ij}^m$  between  $X_i^m$  and  $X_j^m$  (m-dimensional pattern vectors) is defined as

$$d_{ij}^m = d[X_i^m, X_j^m] = \max_{k \in (0, m-1)} |u(i+k) - u(j+k)|$$

and

$$X_i^m = (x_i, x_{i+\tau}, \dots, x_{i+(m-1)\tau})$$

$$(i = 1, 2, \dots, N - (m-1)\tau)$$

The symbol  $r$  represents a predetermined tolerance value, which is defined as

$$r = k \cdot \text{std}(T)$$

where  $k$  is a constant ( $k > 0$ ), and  $\text{std}(T)$  represents the standard deviation of the signal. The two patterns  $i$  and  $j$  of  $m$  measurements of the signal are similar if the distance  $d_{ij}^m$  between any pair of corresponding measurements of  $X_i^m$  and  $X_j^m$  is less than or equal to  $r$ .

## 2.5 SampEn algorithm

The SampEn of a signal of length  $N$   $(x_1, x_2, \dots, x_N)$  is defined as:

$$SampEn(m, r, N) = -\ln \left[ \frac{U^{m+1}(r)}{U^m(r)} \right]$$

where

$$U^m(r) = [N - m\tau]^{-1} \sum_{i=1}^{N-m\tau} C_i^m(r) \quad (3)$$

and

$$C_i^m(r) = \frac{1}{N - (m+1)\tau} \sum_{j=1}^{N-m\tau} \Theta(d_{ij}^m - r) \quad (4)$$

In Eq. (3),  $N$  is the number of time points;  $m$  specifies the pattern length and  $\tau$  is the time delay. In Eq. (4), the symbol  $\Theta$  is the Heaviside function, given as

$$\Theta(z) = \begin{cases} 1 & \text{if } z \leq 0 \\ 0 & \text{if } z > 0 \end{cases}$$

The distance  $d_{ij}^m$  between  $X_i^m$  and  $X_j^m$  ( $m$ -dimensional pattern vectors) is defined as

$$d_{ij}^m = d[X_i^m, X_j^m] = \max_{k \in (0, m-1)} |u(i+k) - u(j+k)|$$

and

$$X_i^m = (x_i, x_{i+\tau}, \dots, x_{i+(m-1)\tau})$$

$$1 \leq j \leq N - m\tau, j \neq i$$

The symbol  $r$  represents a predetermined tolerance value, which is defined as

$$r = k \cdot \text{std}(T)$$

where  $k$  is a constant ( $k > 0$ ), and  $\text{std}(z)$  represents the standard deviation of the signal. The two patterns  $i$  and  $j$  of  $m$  measurements of the signal are similar if the distance  $d_{ij}^m$  between any pair of corresponding measurements of  $X_i^m$  and  $X_j^m$  is less than or equal to  $r$ .

## 2.6 fApEn algorithm

Lotfi Zadeh introduced the concept of “fuzzy sets” and proposed the set membership idea to make suitable decisions in an environment of imprecision and uncertainty [40]. In the physical environment, boundaries between classes are often not sharply defined, which makes it difficult to classify an input signal. Zadeh’s theory provided a mechanism by which an input signal can be classified, where a membership degree introduced by a fuzzy function  $u_z(x)$ , associates each point  $x$  with a real number in the range  $[0, 1]$  [15]. As the value of  $u_z(x)$  gets closer to unity, the higher the membership grade of  $x$  in the set  $\mathbf{Z}$  [15]. The fuzzy membership function  $u(d_{ij}^m, r)$  is used in fApEn to obtain a fuzzy measurement of the similarity between  $X_i^m$  and  $X_j^m$  based on their shapes. As the hard boundary of the Heaviside function softens due to the fuzzy membership function, the points get closer to each other and become more similar [15].

The fApEn algorithm for a signal of length  $N$   $(x_1, x_2, \dots, x_N)$  is defined as:

$$fApEn(m, r, N) = \Phi^m(r) - \Phi^{m+1}(r)$$

where

$$\Phi^m(r) = [N - (m-1)\tau]^{-1} \sum_{i=1}^{N-(m-1)\tau} \ln[C_i^m(r)] \quad (5)$$

and

$$C_i^m(r) = \frac{1}{N - (m-1)\tau} \sum_{j=1}^{N-(m-1)\tau} D_{ij}^m \quad (6)$$

In Eq. (5),  $N$  is the number of time points;  $m$  specifies the pattern length and  $\tau$  is the time delay. In Eq. (6),  $D_{ij}^m$  is determined by a fuzzy membership function, which uses an 'automatic' mirrored quadratic function (where the fuzzy width is set automatically based on  $r$ ).  $D_{ij}^m$  is given as

$$D_{ij}^m = u(d_{ij}^m, r)$$

where the distance  $d_{ij}^m$  between  $X_i^m$  and  $X_j^m$  ( $m$ -dimensional pattern vectors) is defined as

$$d_{ij}^m = d[X_i^m, X_j^m] = \max_{k \in \{0, m-1\}} |u(i+k) - u0(i) - (u(j+k) - u0(j))|$$

and

$$X_i^m = \{u(i), u(i+1), \dots, u(i+m-1)\} - u0(i)$$

$$(i = 1, 2, \dots, N - (m-1)\tau)$$

Here  $u_0(i)$  is a base line value

$$u_0(i) = \frac{1}{m} \sum_{j=0}^{m-1} u(i+j)$$

The symbol  $r$  represents a predetermined tolerance value, which is defined as

$$r = k \cdot \text{std}(T)$$

where  $k$  is a constant ( $k > 0$ ), and  $\text{std}(z)$  represents the standard deviation of the signal. The degree of similarity between the two patterns  $i$  and  $j$  of  $m$  measurements of the signal is determined by the fuzzy membership function,  $\mu(d_{ij}^m, r)$ , a function of the distance between any pair of corresponding measurements of  $X_i^m$  and  $X_j^m$ , with respect to the tolerance parameter  $r$ .

The fuzzy membership function used in this study is based on a pair of quadratic curves arranged in a ‘mirror image’ to produce a sigmoid shape. The basic equation is given below as a function of  $x = \text{distance} / r$ :

$$\mu_{\text{quadratic}}(x) = \begin{cases} 0 \leq x \leq 1: \frac{1}{2}(2 - x^2) \\ 1 < x \leq 2: \frac{1}{2}(2 - x)^2 \end{cases}$$

An additional (optional) feature was added, to provide an ‘automatic’ adjustment of fuzzy width as a function of  $r$ , as introduced by Xiong et al. [41].



## 2.7 Computation of fApEn and SampEn

Whole brain fApEn and SampEn were computed for each of the 86 healthy adults of the ICBM resting state dataset using  $m=2$ , the optimal  $r$  values ( $r = 0.25$  for fApEn and  $r = 0.30$  for SampEn, see Appendix A), multiplied by the SD of the fMRI signal,  $\tau = 1$  and 128 fMRI volumes. The purpose of using a default value of  $\tau = 1$  is to reduce the effect of autocorrelation in the fMRI time series when comparing adjacent points. Whole brain fApEn and SampEn maps were generated on a voxel by voxel basis using the same approach as Sokunbi et al. [2] on a MATLAB and C platform. A threshold of 0.1 times the maximum signal was used to exclude voxels being calculated outside the brain. The mean whole brain fApEn and SampEn values of each subject was computed.

## 2.8 Statistical analysis

All statistical tests were performed using International Business Machines Corporation (IBM) Statistical Package for Social Sciences (SPSS 20.0; New York, USA) software.

The fApEn and SampEn maps of each subject were normalised to a standard echo planar imaging (EPI) template, and regional (spatial) correlation analyses were performed between the fApEn maps and age, and the SampEn maps and age for the whole sample using the multiple regression approach in SPM8 at a family-wise error (FWE) corrected cluster level significance of  $p < 0.05$  and threshold  $p = 0.005$ . Also, the two-sample t-test in SPM8 was used to investigate the interaction between age and sex for the male and female samples, for fApEn and SampEn, at a family-wise error (FWE) corrected cluster level significance of  $p < 0.05$  and threshold  $p = 0.005$ .

Using the Wake Forest University (WFU) PickAtlas tool version 2.5.2, we extracted the tissue types and the default mode brain regions from the fApEn age correlation maps.

### 3. Results

The mean whole brain fApEn value of the male sample was not significantly ( $p>0.05$ ) higher than that of the female sample. When the general linear model analysis (GLM) was performed in SPSS, the GLM showed that there was a main effect of age ( $p<0.001$ ), there was no main effect of sex ( $p=0.561$ ) and there was no interaction between age and sex ( $p=0.174$ ). When the main effect of age was corrected for using the general linear model in SPSS, the mean whole brain fApEn difference between the male and female samples was very close to the level of statistical significance ( $p=0.055$ ). Also, the mean whole brain SampEn value of the male sample was not significantly ( $p>0.05$ ) higher than that of the female sample. When the GLM was performed in SPSS, it showed that there was neither a main effect of age ( $p=0.432$ ) nor sex ( $p=0.946$ ) and no interaction between age and sex ( $p=0.764$ ). When the main effect of age was corrected for, the mean whole brain SampEn difference between the male and female sample was not significant ( $p>0.05$ ). Table 1 shows the mean entropy differences while table 2 shows the main effect and interaction analyses.

A significant ( $p<0.001$ ) negative correlation ( $r = -0.472$ ) was obtained between the mean whole brain fApEn values and the age of the whole sample. This decline is depicted by Figure 1(A), which imply that fApEn decrease with age. For SampEn analysis, a negative correlation ( $r = -0.099$ ) was obtained at a non-significant p-value of 0.367 between the mean

whole brain SampEn values and the age of the whole sample. This is as shown in Figure 1(B). Here, SampEn also decreases with age but the results are not significant. Table 3 entails the mean fApEn and SampEn measures for the whole ICBM resting state dataset and their correlation with age.

To investigate regional (spatial) correlations between the whole brain fApEn maps and age, and the whole brain SampEn maps and age, we performed multiple regression analyses in SPM8 with a family-wise error (FWE) corrected cluster level significance of  $p < 0.05$ . Again, fApEn portrayed a significant ( $p < 0.05$ ) negative correlation with age, for the whole sample as shown by the rendered images in Figure 2. The frontal, parietal, limbic, temporal and cerebellum anterior lobes were discriminated. See Table 4 for a list of the discriminated brain regions. There was no interaction between age and sex for the whole brain fApEn maps ( $p > 0.05$ ). We did not find any significant correlations between the whole brain SampEn maps and age for the whole sample. Also, there was no interaction between age and sex for the whole brain SampEn maps ( $p > 0.05$ ).

Figure 3(A) and 3(B) show that the fApEn of gray and white matter portrayed significant ( $p < 0.05$ ) negative correlations with age. As expected, the fApEn of the cerebrospinal fluid was not significant ( $p = 0.097$ , extent of 19). The negative fApEn-age correlation in white matter ( $r = -0.687$ ) and gray matter ( $r = -0.662$ ) were both significant ( $p = 0.01$ ) and the mean fApEn of white matter ( $0.8266 \pm 0.0076$ ) was significantly ( $p < 0.001$ ) higher than the gray matter ( $0.8181 \pm 0.0082$ ) (Figure 3(C)).

The regions of the default mode network that demonstrated significant ( $p < 0.05$ ) negative fApEn correlations with age were the Precuneus (cluster extent of 1237), posterior cingulate

(cluster extent of 99), medial prefrontal cortex (cluster extent of 392) and the parietal cortex (cluster extent of 192) as shown in the rendered images of Figure 4(A) to 4(D) respectively.

#### 4. Discussion

In this study, we have presented a method for the implementation of fApEn on fMRI data. Here, we investigated the performance and characteristics of fApEn in comparison to SampEn on fMRI signal complexity. Our initial analysis, on a small sample of two groups of ten healthy younger adults and ten healthy older adults that are significantly ( $p < 0.001$ ) different in age showed that fApEn demonstrated excellent performance in discriminating the younger from the older adults, while SampEn performance in discriminating between both groups was good.

In the whole ICBM data set analyses consisting of 86 subjects, the results of the mean whole brain analysis showed that only fApEn demonstrated significant ( $p < 0.05$ ) decline with age of the whole sample. The results of the mean whole brain SampEn analysis also exhibited decline with age, but the association was not significant ( $p > 0.05$ ). Also, only the difference of the mean whole brain fApEn of the males and females after adjusting for the main effect of age was very close to the level of statistical significance ( $p = 0.055$ ), with the males showing slightly higher fApEn than the females. The difference of the mean whole brain SampEn of the males and females after adjusting for the main effect of age was not significant ( $p > 0.05$ ). Here again, fApEn demonstrated superior discriminatory ability than SampEn. In the regional (spatial) analyses of the whole sample, again only the result of fApEn was significant. fApEn showed a significant ( $p < 0.05$ ) negative correlation with age for the whole sample. In a study

by Anokhin et al. [42], they concluded that EEG dimension steadily increase with age (7 to 60 years) and that during maturation (7 to 25 years) the maximum gain in complexity occurs over the frontal associative cortex. An MEG study [43] suggested that such uninterrupted complexity increase with age (7 to 60 years) observed in Anokhin's study [42] may be explained by the characteristics of the sample. In the study by Fernandez et al. [43], their sample included subjects between the sixth and eighth decades of life, and a linear decrease of complexity with age was observed.

In another MEG study of healthy subjects of age 7 to 84 years, the complexity values increase from infancy to adolescence-early adulthood and then tend to slowly decrease [44]. In view of the foregoing, it is reasonable to appreciate the results of our fMRI sample composed of young adults (19 years) to older adults (85 years) where fApEn values decrease from early to late adulthood. According to the Goldberger/Lipsitz model for robustness [35; 36, 37, 1], healthier and more robust systems exhibit more complexity in their physiological output and system complexity decrease with age. Our results are consistent with this model, where the young adult sample of this study exhibited more complex output patterns than their older counterparts and the fMRI signal complexity significantly decreased with age.

The observed fApEn – age correlation in this study showed that white and gray matter correlations with age were both significant and the mean fApEn of white matter was significantly higher than the gray matter. Recently, Liu et al found a similar trend where the mean ApEn values in white matter were significantly ( $p < 0.05$ ) higher than those of gray matter at three different echo times (TE) of 20, 35 and 50 ms [45]. They suggested that noise alone cannot fully account for this effect since the lowest ApEn was observed at the TE of 35ms instead of the predicted 50 ms [45]. With age, white matter cerebrovascular reactivity

response is greater and faster, and is opposite to the changes seen in gray matter [46]. Lu et al. [47] observed age related cerebral blood flow increase in bilateral white matter regions of frontal and parietal lobes but could not explain the physiological mechanism responsible for this effect. More research will be needed to study and understand the biophysical mechanisms underlying the relationship between tissue types and BOLD fMRI entropy. The ageing effect was also observed at some regions of the default mode network which was more pronounced at the precuneus.

Vascular (blood vessel), hemodynamic response function and some systemic changes such as noise may occur in the ageing brain which is more pronounced in group comparisons across the life span [48]. Recently, Tsvetanov et al [49] used resting state fMRI to correct for age differences in vascular reactivity. By using resting state BOLD fMRI data in our study, we have inherently corrected for vascular changes in the ageing brain. Other confounds mentioned above may be controlled for by improvement in experimental designs, smoothing, use of appropriate statistical tests and censoring outliers [48]. Confounds such as cardiac, respiratory and white noise influences may be attenuated by filtering and discriminated by entropy measures as we have done in this study. We have previously discussed the interaction of entropy and noise elsewhere [26].

In the course of these analyses, our investigations were limited to the age and sex only of the sample, and as a result we were unable to investigate further, other confounding factors that may affect the ability of an individual to adapt to the changing demands of normal ageing, such as baseline intelligence or personality. Further studies would be needed to investigate other confounds of fMRI signal complexity. Also, our study is limited by its cross sectional nature; a longitudinal study would better explain the evolution of an individual's signal

complexity across the adult life span. Other potential weakness of this study includes the relatively small sample size of 86 subjects. Further analysis is also required to identify the causal origins of this loss in complexity and if this decline with age can explain individual differences in cognitive performance with age and disease. There are other variants of ApEn and SampEn which can be applied as univariate (single scale entropy), bivariate (cross-fuzzy entropy: C-FuzzyEn and cross-sample entropy: C-SampEn) [50] and multivariate (multiscale entropy) measures. These variants of ApEn and SampEn may give better interesting results and as such will be subjects of future investigations.

This study provides the very first results of fMRI signal complexity analysis using fApEn. Our results are consistent with the Goldberger/Lipsitz model for robustness where healthier and more robust systems exhibit more complexity in their physiological output and system complexity decrease with age. Explicitly, our results suggest that, as we age, changes in patterns of brain activity occur that can be measured using fMRI and entropy. In comparison to the well-known and established SampEn, fApEn demonstrated superior discriminatory ability, detecting subtle patterns and signal changes which were not detected by SampEn. This study has shown that fApEn is a sensitive, specific and accurate new method for the analysis of fMRI data.

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([https://www.nitrc.org/projects/fcon\\_1000/](https://www.nitrc.org/projects/fcon_1000/)). M.O. Sokunbi was supported by an MRC grant G1100629.

### **Competing interests**

There are no competing interests

### **Ethical Approval**

The International Consortium for Brain Mapping (ICBM) resting state dataset made publicly available in the 1000 Functional Connectomes project was used for this investigation. The study was approved by the local research ethics committee. Information regarding this dataset is available at [https://www.nitrc.org/projects/fcon\\_1000/](https://www.nitrc.org/projects/fcon_1000/).



## Appendix A

### Determination of the optimal tolerance value, $r$ for fApEn and SampEn

In order to determine the optimal tolerance value,  $r$  for robust computations of SampEn and fApEn, we used the same approach in [26]. We evaluated the ability of fApEn and SampEn to discriminate the younger (5 male, mean age  $(22.40 \pm 3.44)$ ) from the older (5 male, mean age  $(69.60 \pm 9.25)$ ) adults using the value of the receiver operating characteristic (ROC) area [51]. We determined the optimal  $r$  value where this discrimination occurs by computing the ROC area for a range of  $r$  values. The ROC area was computed from the mean whole brain fApEn and SampEn values of each subject using a robust value of  $m=2$  [52], data length  $N=128$  and by varying the  $r$  value from 0.05 to 0.5 at intervals of 0.05. The optimal  $r$  values for fApEn and SampEn were obtained at 0.25 and 0.30 respectively. Fig. A1 (A) and (B) show the ROC curves for fApEn and SampEn respectively. Fig. A1(C) shows the graphs for the determination of the optimal  $r$  values for fApEn and SampEn.

The ROC areas corresponding to the optimal  $r$  values of 0.25 (fApEn) and 0.30 (SampEn) were 0.930 and 0.833 respectively. This implies that the ability of fApEn to effectively discriminate the younger from the older adults was excellent, while the discriminatory ability of SampEn between both groups was good. The sensitivity, specificity and accuracy of fApEn at the optimal  $r$  value (0.25) were 90%, 90% and 90% respectively, at a threshold of 0.8328. Also, the sensitivity, specificity and accuracy of SampEn at its optimal  $r$  value (0.30) were 66.70%, 80% and 73.35% respectively, at a threshold of 1.6816. The mean whole brain fApEn and SampEn values of the younger adults were significantly ( $p < 0.05$ ) higher than those of the corresponding older adults respectively, at the optimal  $r$  values.

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**Table 1.** Mean differences for fApEn and SampEn measures

	Males	Females	Significance (p-values)
Number of subjects	41	45	
Age (years)	44.66 ± 15.358	43.76 ± 20.130	p = 0.817
fApEn	0.8343±0.0049	0.8321±0.0076	p = 0.114
fApEn after adjusting for age	0.8340±0.0093	0.8320±0.0093	p = 0.055
SampEn	1.6923±0.0571	1.6797±0.0646	p = 0.341
SampEn after adjusting for age	1.6920±0.0927	1.6800±0.0835	p = 0.329



**Table 2.** Main effect and interaction analyses  
for fApEn and SampEn measures

	Significance (p-values)
Main effect of age for fApEn GLM analysis	p < 0.001
Main effect of sex for fApEn GLM analysis	p = 0.561
Interaction between age and sex (age*sex) for fApEn GLM analysis	p = 0.174
Main effect of age for SampEn GLM analysis	p = 0.432
Main effect of sex for SampEn GLM analysis	p = 0.946
Interaction between age and sex (age*sex) for SampEn GLM analysis	p = 0.764

**Table 3.** ICBM sample mean, fApEn and  
SampEn correlation with age

	ICBM sample	Significance (p-values)
Sex(M/F)	41/45	
Age (years)	44.19±17.92	
fApEn	0.8331±0.0065	
SampEn	1.6857±0.0611	
Correlation of fApEn with age	r = -0.472	p<0.001
Correlation of SampEn with age	r = -0.099	p = 0.367

**Table 4.** Multiple regression analysis of fApEn with age for the whole sample. Location coordinates are those of the peak significance in each region (threshold  $p=0.005$ , FWE corrected cluster  $p<0.05$ ).

	<b>Cluster number and extent</b>	<b>Brain region</b>	<b>Talairach coordinate (XYZ)</b>	<b>Brain label</b>	<b>Tissue type</b>	<b>Cluster p value (FWE corrected)</b>	<b>Voxel t value</b>
The whole sample	Cluster 1	Parietal Lobe	-58 -18 34	Left Postcentral Gyrus	Gray Matter	$p < 0.001$	6.19
	Extent =	Parietal Lobe	-26 -54 56	Left Sub-Gyral	White Matter	$p < 0.001$	5.72
	35,535	Frontal Lobe	-32 -2 62	Left Middle Frontal Gyrus	White Matter	$p < 0.001$	5.60
	Cluster 2						
	Extent =						
	667	Cerebellum	10 -46 0	Right Culmen		$p = 0.037$	4.35
		Anterior Lobe					
		Limbic Lobe	8 -48 8	Right Posterior Cingulate	White Matter	$p = 0.037$	4.15
		Temporal Lobe	24 -62 14	Right Sub-Gyral	White Matter	$p = 0.037$	3.82

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Figure 1: Regression curve estimation between entropy and age for the whole sample, here, entropy decrease with an increase in the age of the sample. (A) Curve estimation between the mean whole brain fApEn ( $m=2$ ,  $r=0.25$ ,  $N=128$ ) and age of the whole sample (B) Curve estimation between the mean whole brain SampEn ( $m=2$ ,  $r=0.30$ ,  $N=128$ ) and age of the whole sample.

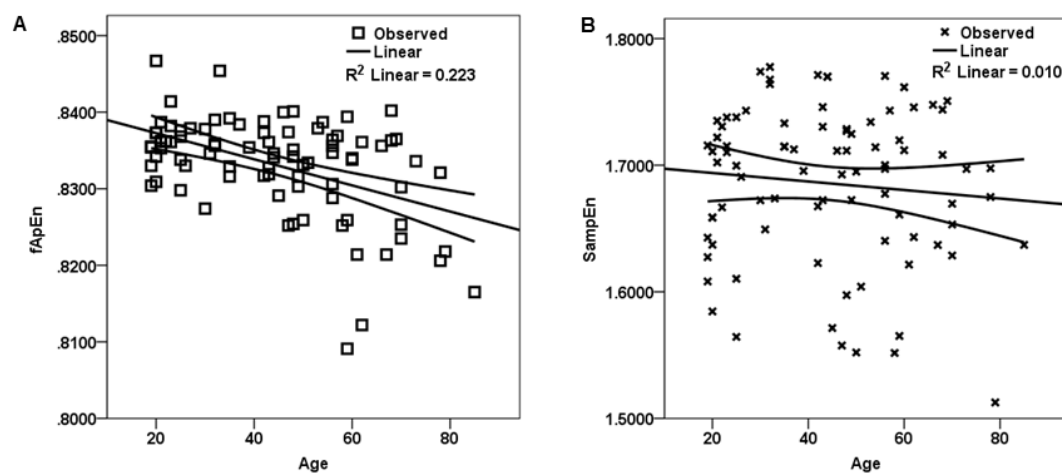
Figure 2: Correlation of fApEn ( $m=2$ ,  $r=0.25$ ,  $N=128$ ) with age for the whole sample. fApEn for the sample decreases as age increases with corresponding brain regions as depicted in the rendered images.

Figure 3: fApEn-age correlation and magnitude in gray and white matter. (A) Rendered images of gray matter fApEn ( $m=2$ ,  $r=0.25$ ,  $N=128$ ) correlation ( $r = -0.662$ ) with age for the whole sample. (B) Rendered images of white matter fApEn ( $m=2$ ,  $r=0.25$ ,  $N=128$ ) correlation ( $r = -0.687$ ) with age for the whole sample. (C) Mean fApEn of white matter ( $0.8266 \pm 0.0076$ ) was significantly ( $p < 0.001$ ) higher than the gray matter ( $0.8181 \pm 0.0082$ ).

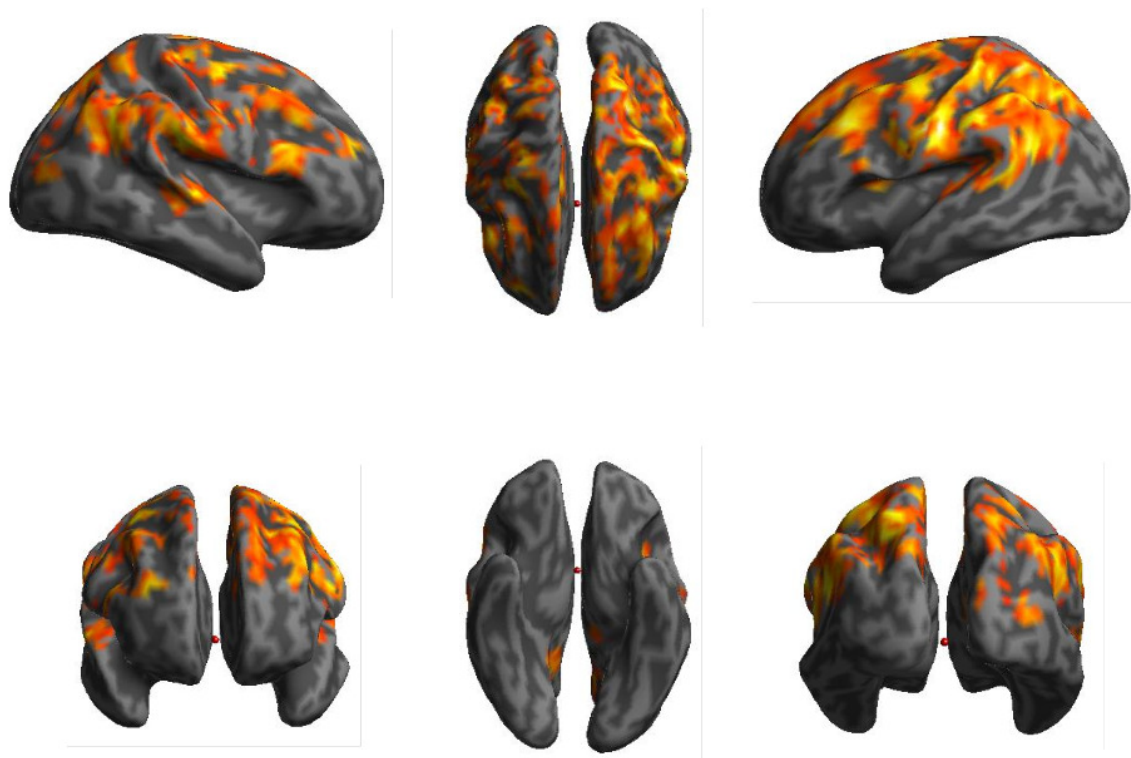
Figure 4: Regions of the default mode network showing a significant negative fApEn correlation with age. (A) The precuneus with a cluster extent of 1237 (B) the posterior cingulate with a cluster extent of 99 (C) medial prefrontal cortex having a cluster extent of 392 and (D) parietal cortex with cluster extent of 192.

Figure A1: ROC analyses portraying fApEn and SampEn discriminatory characteristics for 20 subjects (A) ROC curves for fApEn. (B) ROC curves for SampEn and (c) ROC area for determining the optimal  $r$  value for fApEn ( $m=2$ ,  $0.05 \leq r \leq 0.5$  at intervals of 0.05,  $N=128$ ) and SampEn ( $m=2$ ,  $0.05 \leq r \leq 0.5$  at intervals of 0.05,  $N=128$ ). The optimal  $r$  values for fApEn and SampEn were obtained at  $r = 0.25$  and  $r = 0.30$  respectively.

839 Figure 1



849 Figure 2



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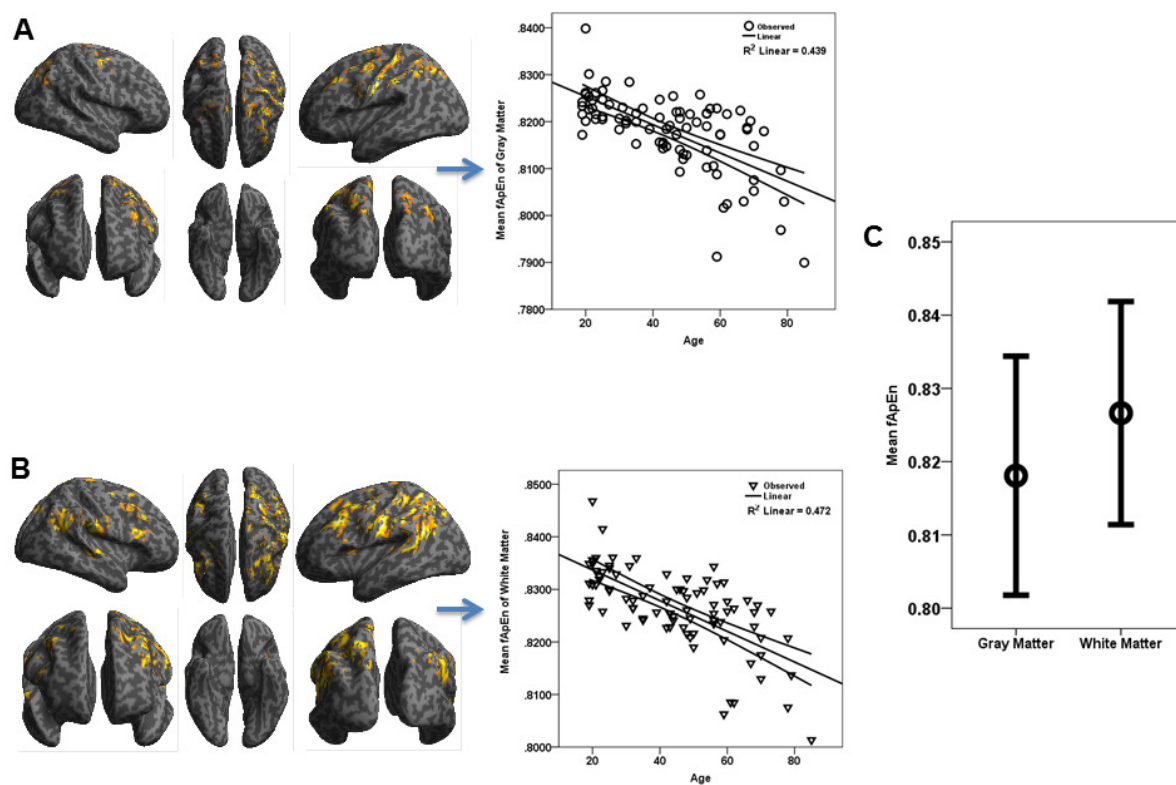
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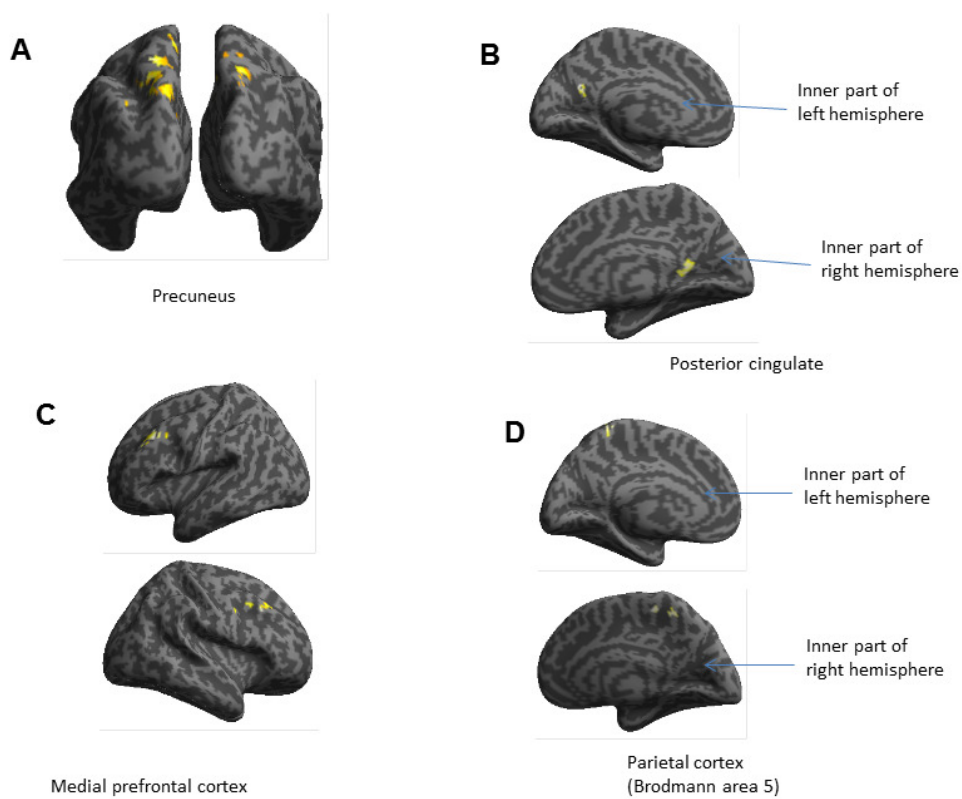
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859 Figure 3





869 Figure 4



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879 Figure A1

